


Populations

1

LIFE on Earth

- **chemical** basis (carbon-based life on water-planet)
 - proteins, sugars, fats, nucleotides
- **genetic** code (DNA)
 - replication, transcription, translation
 - four bases (2 bit (binary digit) code)
- **cellular** organization (membranes, organelles, nuclei)
 - basic units of life
- **evolution** (natural selection, survival of fittest)
 - mutation, recombination
- **symbioses** (living together)
 - organelles (SET)
 - organisms (life styles)

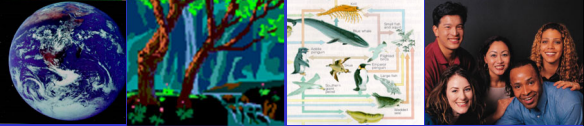
→ collective co-existence (**ecology**)



2

Ecology (hierarchy)

- **biosphere** (all environments on Earth inhabited by life)
- **ecosystems** (all living and non-living things within given area)
(matter recycles while energy flows through)
- **communities** (all species within given area)
(interactions between species, e.g. food chains, competition, predation, herbivory, disease)
- **populations** (all individuals of single species)
(single species distribution and abundance)



3

Review - BIOLOGY

(study of life)

- **organisms**
 - species stage-classified (matrices)
 - biodiversity species-area (power fn)
- **populations**
 - growth unconstrained (exponential fn)
 - constrained (logistic model)
 - interactions predator-prey (DE) [L-V]
 - epidemiology (DE) [SIR]

4

Population ecology

- **distribution**
 - temporal (any time frame, but esp. seasonal)
 - spatial (any space, but esp. regional)
- **abundance**
 - size (number)
 - density (number/area)
 - concentration (number/volume)
 - intensity (e.g. number parasites/host)
 - prevalence (e.g. proportion infected)
 - incidence (change in prevalence over time)

5

Population growth

- vital statistics of populations (changes over time)
- individuals join (births and immigration)
- individuals leave (deaths and emigration)

$$P_2 = P_1 + (\text{births} + \text{immigration}) - (\text{deaths} + \text{emigration})$$

- assume closed population (no migration)

$$P_2 = P_1 + (\text{births} - \text{deaths})$$

that is, population is proportionate to:

- current size (P_t)
- growth rate (r) (= birth rate – death rate)

6

Population growth

Seal lecture room with 100 students inside

Count changes in number over one year

Five births

Two deaths

No escapees (closed pop.)

$$\text{POP}_{(2012)} = \text{POP}_{(2011)} + \text{births} - \text{deaths}$$

$$\text{POP}_{(2012)} = 100 + 5 - 2 = \underline{103}$$

7

Population growth

Alternatively, determine rates (change over one year):

birth rate = $5 / 100 = 0.05$ (= 5%)

death rate = $2 / 100 = 0.02$ (= 2%)

Growth rate = birth rate - death rate

$$= 0.05 - 0.02 = 0.03 \quad (= 3\%)$$

$$\text{POP}_{(2012)} = \text{POP}_{(2011)} \times \text{growth rate}$$

$$\text{POP}_{(2012)} = 100 \times 1.03 = \underline{103}$$

⇒ POP now = POP previous × growth rate sounds ominously mathematical!

8

Population growth rate, R

population size

time

R > 1 increase

R = 1 ZPG

R < 1 decrease

9

Population characters

- demography (categorize!)
 - biology (age, sex, breed, size ...)
 - other (income, postcode, religion, ...)
- life tables
 - age/stage-structure, numbers
 - births, deaths, migrations
- survivorship curves
 - life expectancy

10

Exemplar: age/stage population structure

Fleas (itchy-scratchy syndrome)

the dangers of not wearing shoes!

11

Flea Life History

egg

↓

larva

↓

pupa

↓

adult

Age (weeks)	Dev. Stage	Number alive	Proportion alive
0-2	eggs	10,000	1.00
3-5	larvae	500	0.05
6-7	pupae	50	0.005
8-20	adults	30	0.003

Survivorship Curve

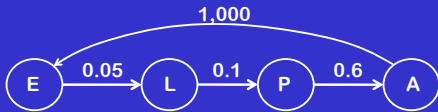
log survivors vs time

12

Stage-structured diagrams

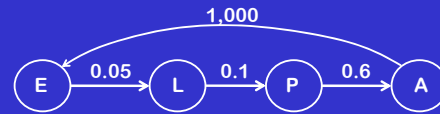
- used to depict life-cycles
- arrows show proportion in transition

Time period	Flea developmental stage	Number alive
1	Eggs	10,000
2	Larvae	500
3	Pupae	50
4	Adults (50% female) (females lay 2,000 eggs)	30



13

Simultaneous equations



$$E_{i+1} = 0 E_i + 0 L_i + 0 P_i + 1,000 A_i = 1,000 A_i$$

$$L_{i+1} = 0.05 E_i + 0 L_i + 0 P_i + 0 A_i = 0.05 E_i$$

$$P_{i+1} = 0 E_i + 0.1 L_i + 0 P_i + 0 A_i = 0.1 L_i$$

$$A_{i+1} = 0 E_i + 0 L_i + 0.6 P_i + 0 A_i = 0.6 P_i$$

14

Matrix operation

$$\begin{aligned} E_{i+1} &= 0 E_i + 0 L_i + 0 P_i + 1,000 A_i \\ L_{i+1} &= 0.05 E_i + 0 L_i + 0 P_i + 0 A_i \\ P_{i+1} &= 0 E_i + 0.1 L_i + 0 P_i + 0 A_i \\ A_{i+1} &= 0 E_i + 0 L_i + 0.6 P_i + 0 A_i \end{aligned}$$

transition matrix

$$\begin{pmatrix} 0 & 0 & 0 & 1,000 \\ 0.05 & 0 & 0 & 0 \\ 0 & 0.1 & 0 & 0 \\ 0 & 0 & 0.6 & 0 \end{pmatrix}$$

15

Matrix multiplication

assume population $N_0 = 100 E, 50 L, 10 P, 2 A$
calculate N_1

$$\begin{pmatrix} 0 & 0 & 0 & 1,000 \\ 0.05 & 0 & 0 & 0 \\ 0 & 0.1 & 0 & 0 \\ 0 & 0 & 0.6 & 0 \end{pmatrix} \times \begin{pmatrix} 100 \\ 50 \\ 10 \\ 2 \end{pmatrix} = \begin{pmatrix} 2,000 \\ 5 \\ 5 \\ 6 \end{pmatrix}$$

16

ALGAL BLOOMS

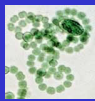
Cyanobacteria (pond scum)

- aquatic swimmers
- with chloroplasts (need sunlight)
- bloom populations (organic-enrichment)
- biotoxic pigments (blue-green algae)



Dairy cows – liver disease – cirrhosis (///alcoholics)

- liver fluke infestation? (no evidence on pm)
- toxicology
 - herbicides X
 - CB hepato-toxins ✓
- causative agents (Annie, Fannie, Mike & Noddy)



(Anabaena, Aphanizomenon, Microcystis, Nodularia)

17

Escherichia coli

- Gram-negative rod bacteria
- up to 10^{12} bacteria per gram faeces (~ 10% wet weight)
- minimum infective dose 10^4 - 10^6
- virulent strains in g-i tract of mammals
 - ETEC = entero-toxigenic *E.c.*
 - EPEC = entero-pathogenic *E.c.*
 - EHEC = entero-haemorrhagic *E.c.*
 - EIEC = entero-invasive *E.c.*
- all rapid growers!!!!



18

Epidemiology?

Like ecologists, epidemiologists seek to understand:

- species **richness** (biodiversity)
- species **abundance** (populations/communities)
- species **distribution** (temporal, spatial)



Study human pathogens = epidemiology
Study animal pathogens = epizootiology

19

Epidemiology/Epizootiology

Study of **occurrence**, **spread** and **control** of diseases
(descriptive) (analytical) (experimental)

- Prevalence (number infected)
- Incidence (change in prevalence over time)
- Distribution (density, intensity, concentration,..)

exhibit longitudinal fluctuations (esp. seasonal)

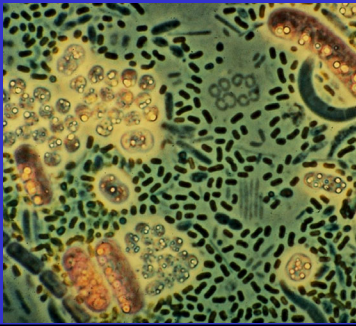
influenced by many factors:

- demographic, socioeconomic, behavioural
- geographic, climatic

20

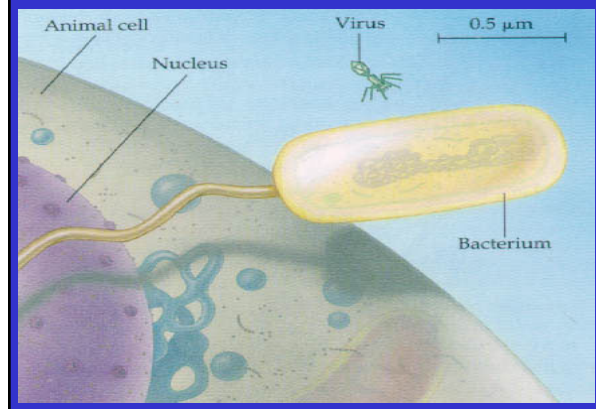
INFECTIOUS DISEASES

What percentage of the world population believes in the GERM theory?



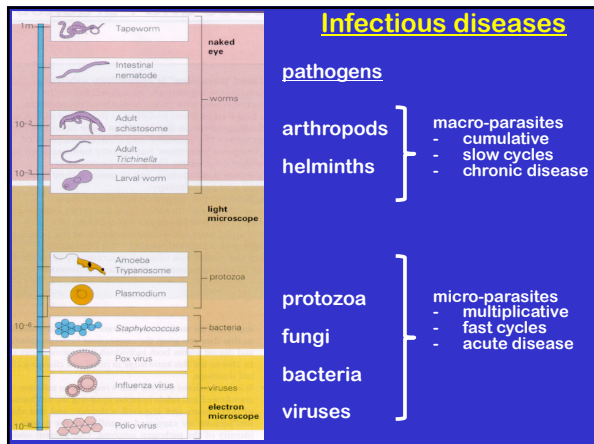
21

Eukaryote - Prokaryote Domains



22

Infectious diseases



23

Epidemiological studies

Four main types:

- | Study Type | Characteristics | Maths |
|---|------------------------------------|------------------------------------|
| • Case series (descriptive) | – index, incidental, miscellaneous | not quantitative |
| • Case control studies (retrospective) | – cases + controls interviewed | statistics
Odds Ratio |
| • Cohort studies (prospective) | – cohort followed forward in time | statistics
Relative Risk |
| • Outbreak studies (predictive) | – rate of change in population | calculus
Differential Equations |

24

OR and RR

	CASES	CONTROLS
EXPOSED	A	B
UNEXPOSED	C	D

Odds Ratio (OR) = $\frac{AD}{BC}$

Relative Risk (RR) = $\frac{A / (A+B)}{C / (C+D)}$

$\gg 1$ causative?
 ~ 1 no association
 $\ll 1$ protective?

25

OUTBREAKS

Pathogens must reproduce themselves to survive (reproduction rate = R)

time

Basic (case) reproduction rate (R_0)
 = average number of secondary infections resulting from primary case in **susceptible** population

26

BUT, nothing is IDEAL

Population varies in susceptibility

- proportion just infected (latent)
- proportion patent (infectious)
- proportion immune (resistant)
- proportion lose resistance (susceptible)
- proportion die
- proportion migrate
- etc

⇒ all influence R_0
 ⇒ need to stipulate model

27

SIR model (long-term immunity)

Identify three states in population Movement shown by differential equations

S = susceptible

dS/dt

↓

I = infectious

dI/dt

↓

R = resistant

dR/dt

↶

28

Infectious Disease Models

Micro-parasites

(viruses, bacteria, protozoa)

- reproduce quickly
- high intensity of infection
- acute transient diseases
- strong protective immunity

population dynamics driven by:

- transmission rate
- recovery rate

SIR model

Macro-parasites

(helminths, arthropods)

- reproduce slowly
- aggregated distribution
- chronic persistent diseases
- little protective immunity

population dynamics driven by:

- exposure to free-living stages
- overdispersion in hosts

HPW model

29

SIR model

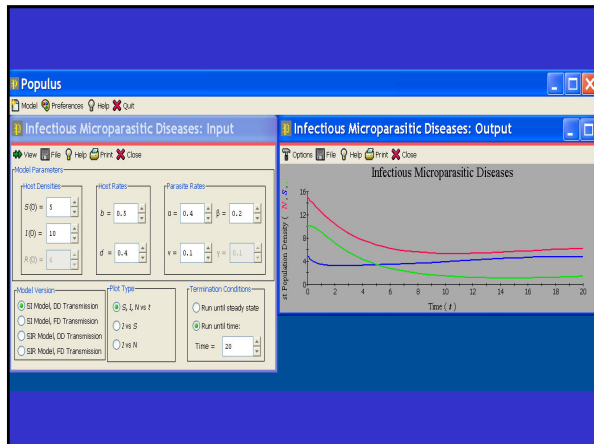
(N = Susceptible + Infected + Recovered/immune)

in out

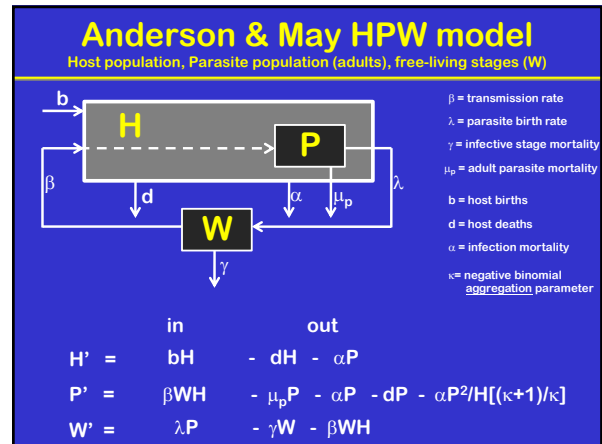
$$\begin{aligned}
 S' &= bN + \gamma R - dS - \beta SI \\
 I' &= \beta SI - dI - \alpha I - \nu I \\
 R' &= \nu I - dR - \gamma R
 \end{aligned}$$

β = infection rate
 ν = recovery rate
 γ = immunity loss
 b = births
 d = deaths
 α = infection mortality

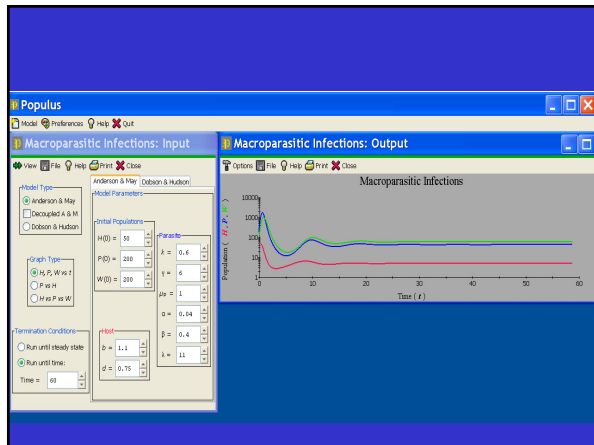
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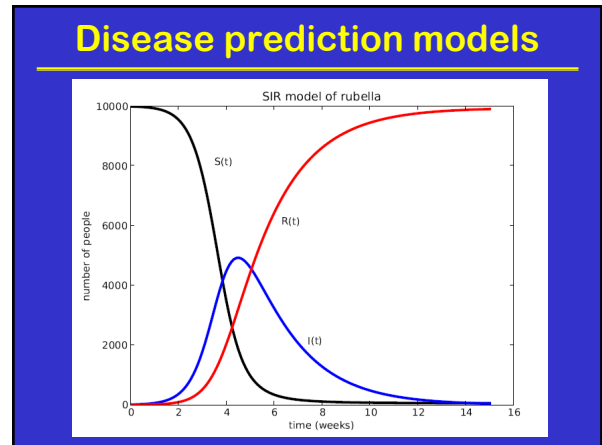
31



32



33



34

Global Burden of Disease

(YLL = morbidity; YLD = morbidity)

Recent shift in distribution of deaths:

- from younger to older ages
- from communicable/maternal/perinatal/nutritional causes to noncommunicable disease causes

Leading causes:

- ischaemic heart disease
- cerebrovascular disease/hypertension
- respiratory infections/COPD
- infectious diseases
- perinatal diseases
- diarrhoeal diseases
- cancer
- road traffic crashes
- diabetes
- kidney diseases

35